



THE UNIVERSITY OF
SYDNEY

Probing the cosmic dipole in the radio sky

RACS-low and NVSS

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The University of Sydney

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Geraint Lewis
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Agenda

Background

- The Cosmological Principle
- CMB (Kinematic) Dipole
- Testing the Principle
- Literature Results

Analysis

- Samples
- Preparation
- Statistics

Results

- Individual
- Joint
- Local Sources

Conclusions



Background

The Cosmological Principle

On very large scales, the Universe **looks the same everywhere** — it is **homogeneous** and **isotropic**.

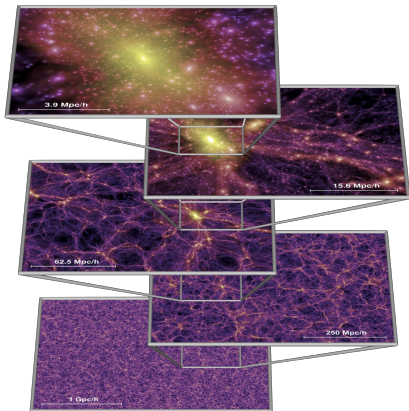


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Foundational assumption in current cosmological framework, e.g. FLRW, Friedmann world models, etc.

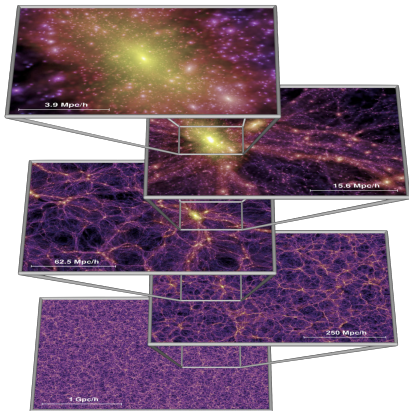


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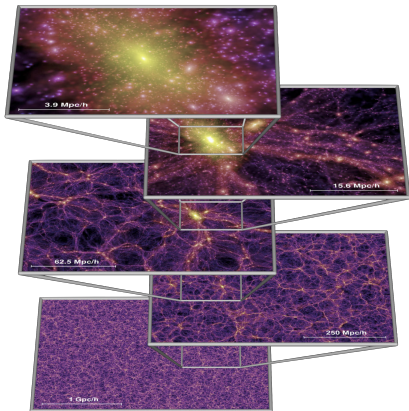


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$$ds^2 = -c^2 dt^2 + a^2(t) \left[\frac{dr^2}{1 - \kappa r^2} + r^2(d\theta^2 + \sin^2 \theta d\phi^2) \right]$$

The Cosmic Microwave Background

- The CMB is remarkably smooth ($\Delta T/T \approx 10^{-5}$).

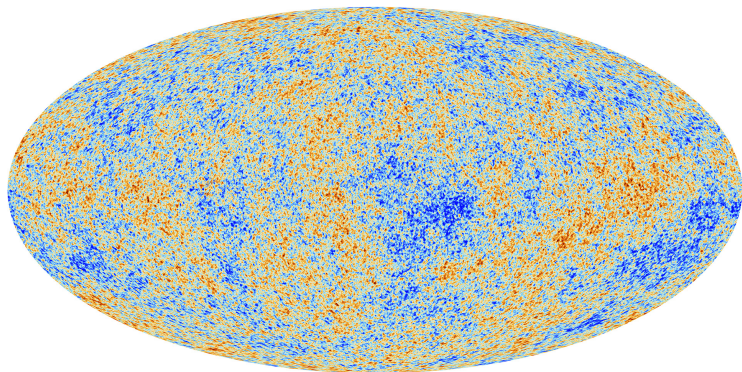


Figure 2: CMB temp. map (dipole subtracted; Planck Collaboration et al., 2020).

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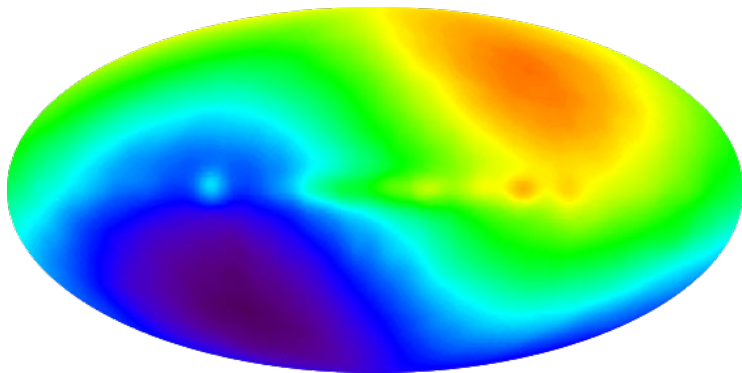


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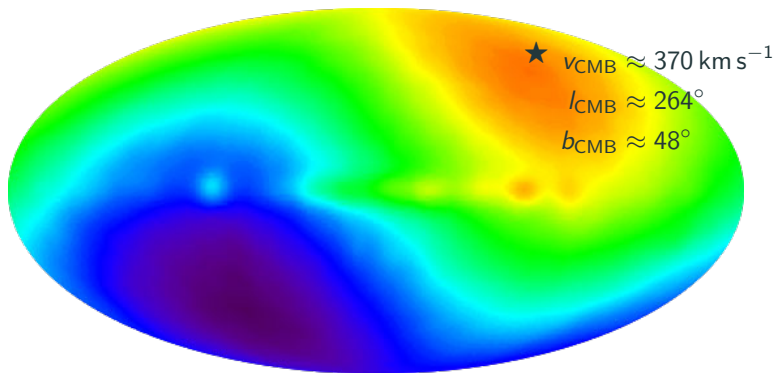


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- CP \rightarrow the dipole-removed frame is the frame of **cosmic rest**.
- *How do we test the CP?*

The Ellis & Baldwin (1984) Test

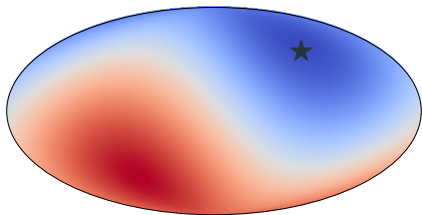


Figure 3: Dipole signal, Doppler shift.

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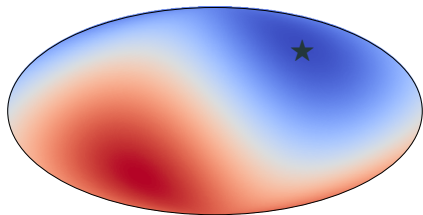


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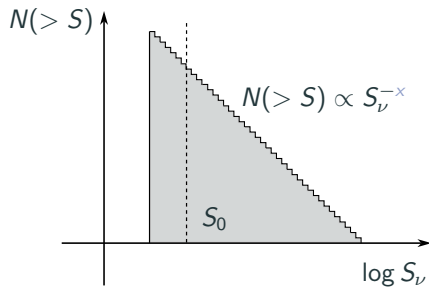


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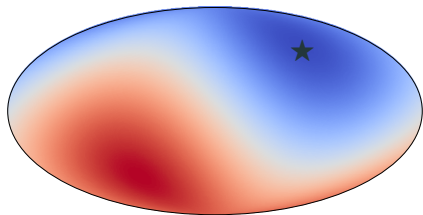


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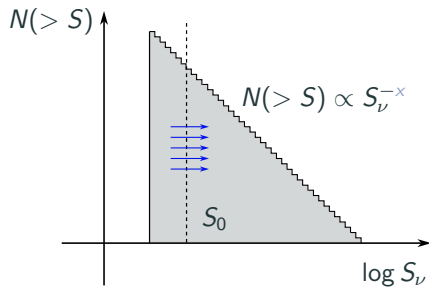


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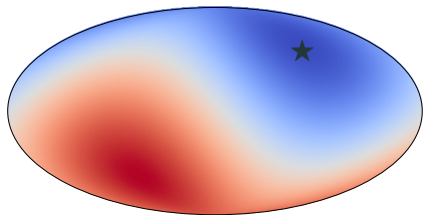


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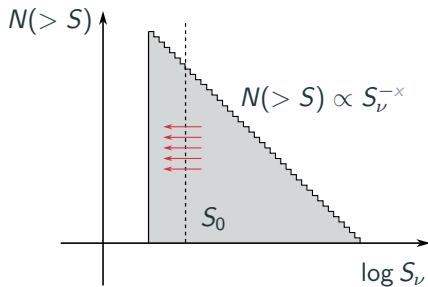


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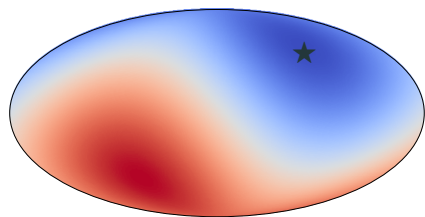


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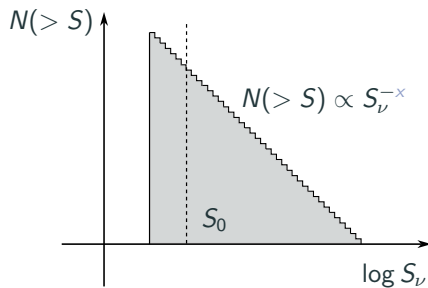


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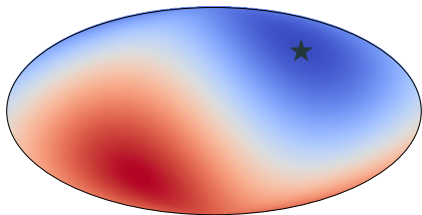


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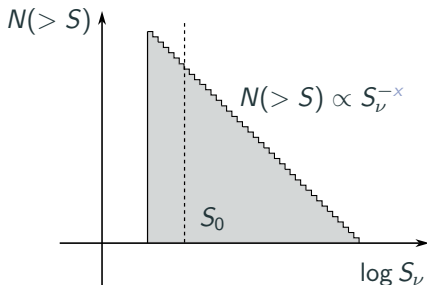


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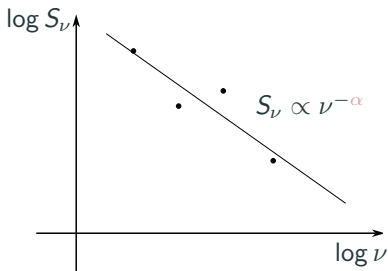


Figure 5: Power law dependence of flux S_ν on frequency ν .

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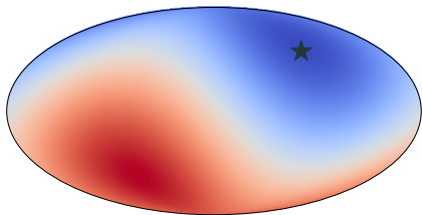


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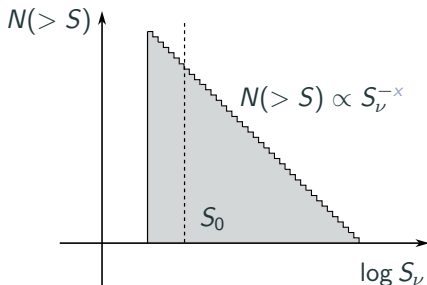


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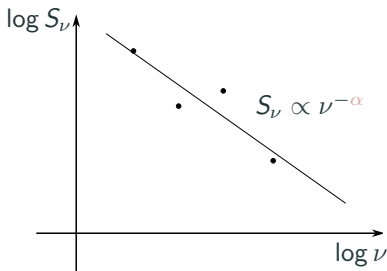


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We use only **special relativity** to derive how our peculiar motion impacts observables — like galaxy surveys.

E&B Relation

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We find a **dipolar modulation** in source density where

$$\mathcal{D} = [2 + x(1 + \alpha)]\beta.$$

$$\alpha = 0.75, x = 1, \beta = v_{\text{CMB}}/c = 0.00123 \implies \mathcal{D} = 0.0046.$$

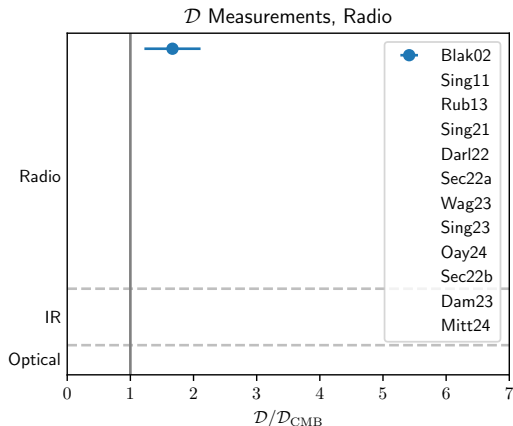
A 0.5% effect!

Measurements of the Cosmic Dipole

$$\mathcal{D}_{\text{CMB}} = \underbrace{[2 + x(1 + \alpha)] \times v_{\text{CMB}}/c}_{\text{expectation}} \quad \text{vs.} \quad \underbrace{N_{\text{cell}} = \bar{N}(1 + \mathcal{D} \cos \theta)}_{\text{reality}}$$

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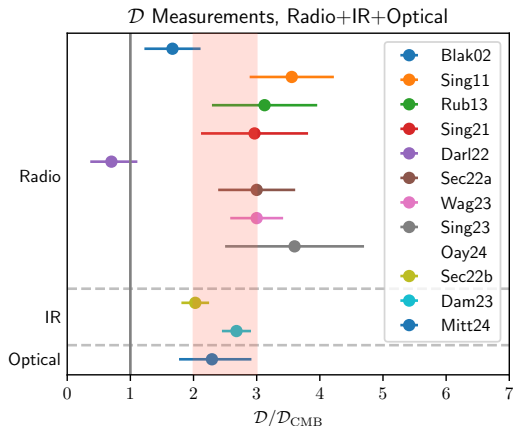
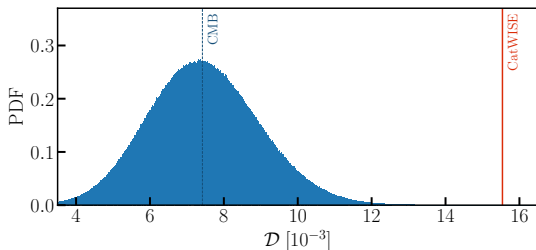


Figure 6: Literature values for \mathcal{D} across radio, optical and near-IR samples (1σ uncertainties). Key samples: **NVSS**, **RACS-low**, **CatWISE2020**, **Quia**.

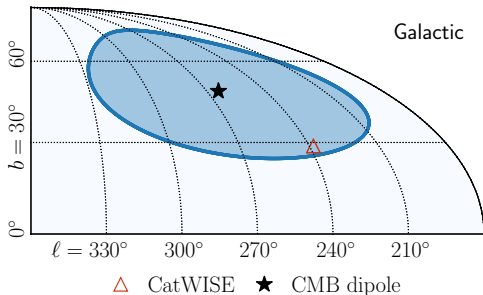
Results of Secret et al. (2021) — IR

Amplitude $\approx \times 2$ larger than CMB expectation at significance of 5σ .



Confirmed by Dam et al. (2023) with a Bayesian approach.

Figure 7: Results from Secret et al. (2021). *Top:* Statistical significance (5σ) of the CatWISE dipole amplitude. *Bottom:* Significance of the direction of the dipole in CatWISE (2σ contour).



Results of Mittal, Oayda & Lewis (2024) — Optical

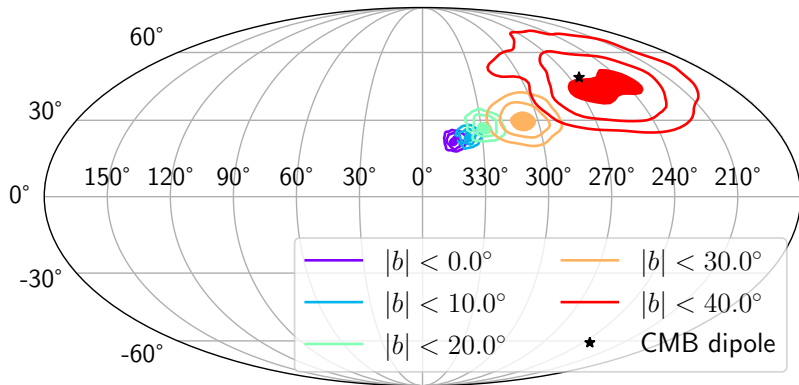


Figure 8: Results from Quaia low ($G < 20.0$) as in Mittal et al. (2024). *Top:* projection of marginal posterior for dipole direction onto the sky. *Bottom:* 2σ credible interval for dipole amplitude by mask choice.

Results of Wagenveld et al. (2023) — Radio

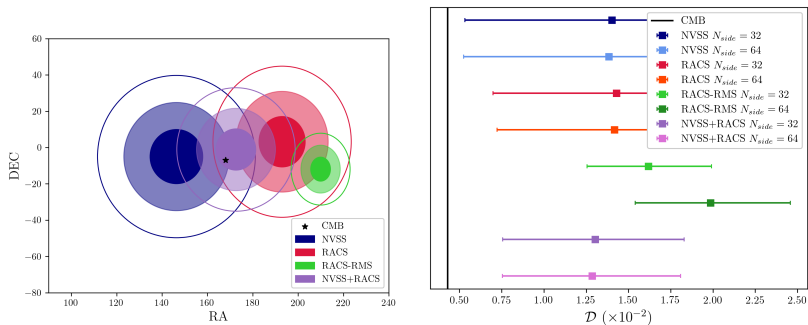


Figure 9: Results of Wagenveld et al. (2023) also point towards an excessive dipole amplitude (but consistent direction).

- ‘W23’ — used as prior likelihood later.
- We also analysed NVSS and RACS-low, but with a different approach.

Why is the dipole amplitude larger than expected?

Analysis

Samples We Tested

NVSS (NRAO VLA Sky Survey):
1993–97, 1.4 GHz, northern sky.

RACS-low (Rapid Australian SKA
Pathfinder Continuum Survey):
2019–20, 887.5 MHz, southern
sky.

Figure 10: *Top:* VLA in New Mexico
(credit: NRAO). *Bottom:* Australian
SKA Pathfinder in Western Australia
(credit: CSIRO).



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- Declination-dependent systematics.
- Contamination from the Galactic plane and bright radio sources.

Preparing NVSS & RACS

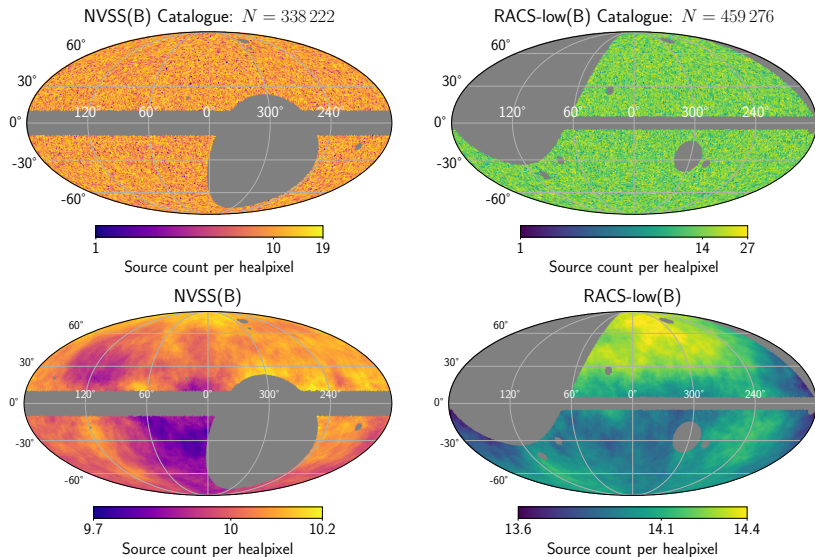


Figure 11: NVSS and RACS-low samples in Galactic coordinates binned into healpixels. *Top:* Raw density maps. *Bottom:* Smoothed density maps.

Cross-matching Local Sources

Remove **nearby structure**, which complicates the picture.

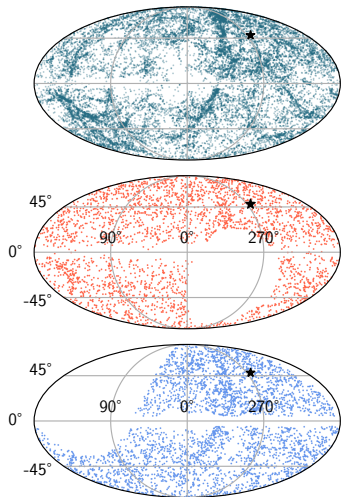


Figure 12: *Top:* 2MRS, $z < 0.02$.
Middle: NVSS. *Bottom:* RACS-low.

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Cross-match NVSS and RACS-low radio sources with counterparts:
2MRS (near-IR); **NED** (radio).

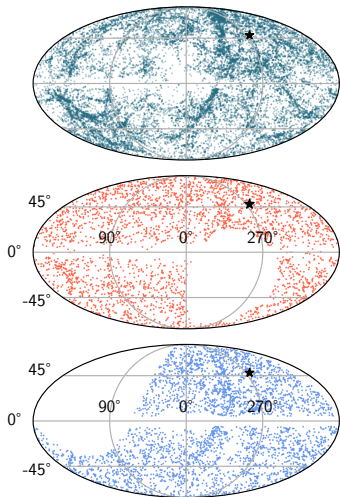


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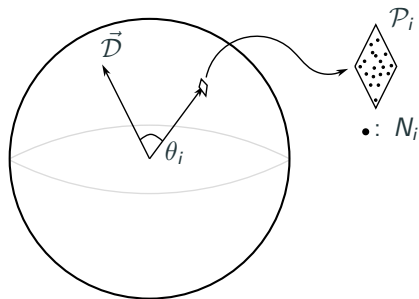


Figure 13: Schematic of pixel \mathcal{P}_i on the celestial sphere with N_i sources (\bullet) near dipole vector \vec{D} .

Dipole vector \vec{D} is a **free parameter**.

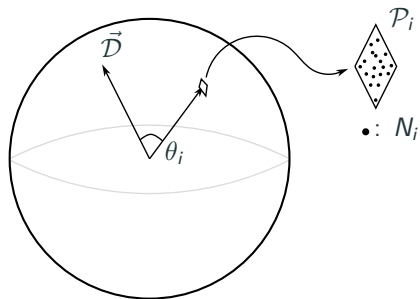


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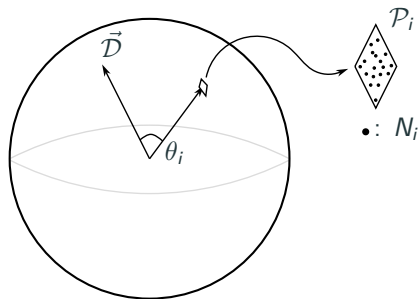


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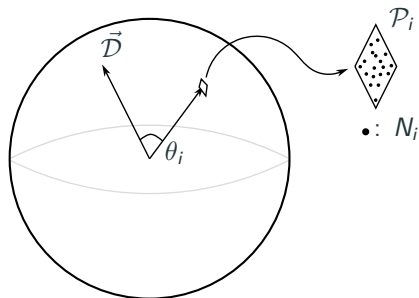


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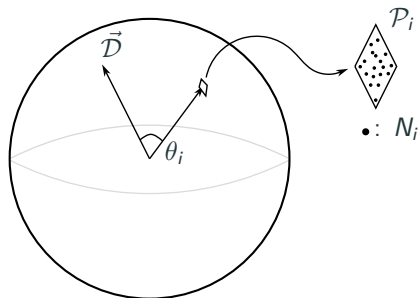


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$$\ln \mathcal{L} = \sum_{i=1}^{n_{\text{pix.}}} N_i \ln \hat{f}_i.$$

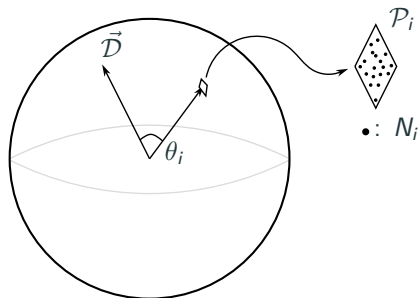


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Use a **Bayesian** statistical approach to infer posterior probability distribution for \mathcal{D} , l and b . Analyse individually and **jointly**.

	Short label	Description
M_0	Null	Monopole
M_1	Free dipole	Free \mathcal{D} , l , b
M_2	Kinematic velocity	\mathcal{D} fixed and free l , b
M_3	Kinematic direction	l , b fixed and free \mathcal{D}
M_4	Kinematic dipole	All parameters fixed to CMB expectation
M_5	W23	\mathcal{D} , l , b from Wagenveld et al. (2023)

Table 1: The six models tested and ranked.

Compare models' explanatory power with **marginal likelihood** $P(\vec{D}|M)$.

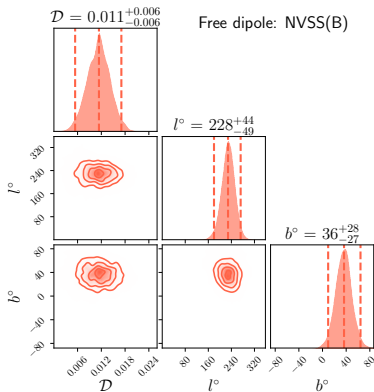
Results


NVSS & RACS: Individual Results

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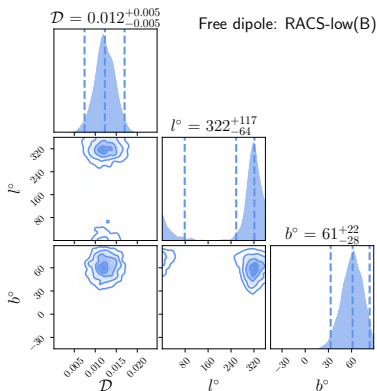
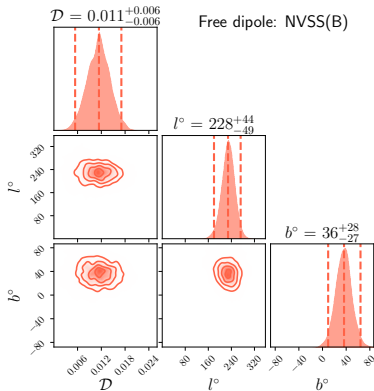
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Model	$\ln B_{i0}$
M_1 Free dipole	3.1
M_3 Kin. direction	4.5
M_4 Kin. dipole	4.8 

NVSS & RACS: Individual Results

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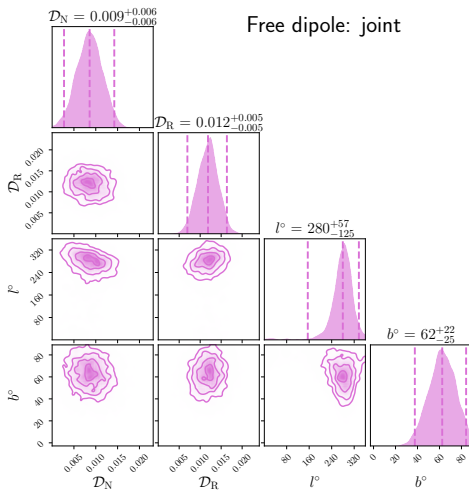
Model	$\ln B_{i0}$
M_1 Free dipole	8.2 
M_3 Kin. direction	7.5
M_4 Kin. dipole	6.6

Joint Analysis: NVSS + RACS-low

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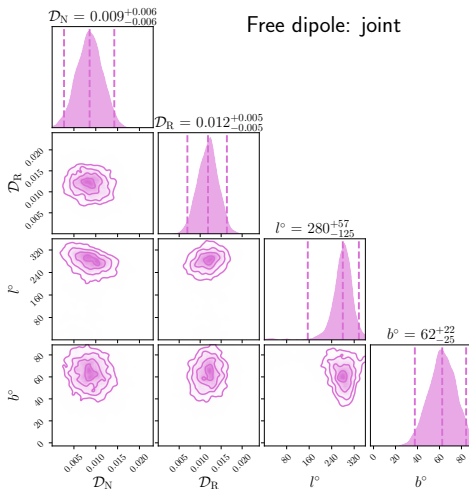
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Model	$\ln B_{i0}$
M_3 Kin. dir.	12.1 
M_4 Kin. dipole	11.4
M_5 W23	17.1 

M_3 (kinematic direction):

$$\mathcal{D}_{\text{NVSS}} \approx (10 \pm 5) \times 10^{-3}$$

$$\mathcal{D}_{\text{RACS}} \approx (11 \pm 5) \times 10^{-3}$$

Joint Analysis: Dipole Position Distribution

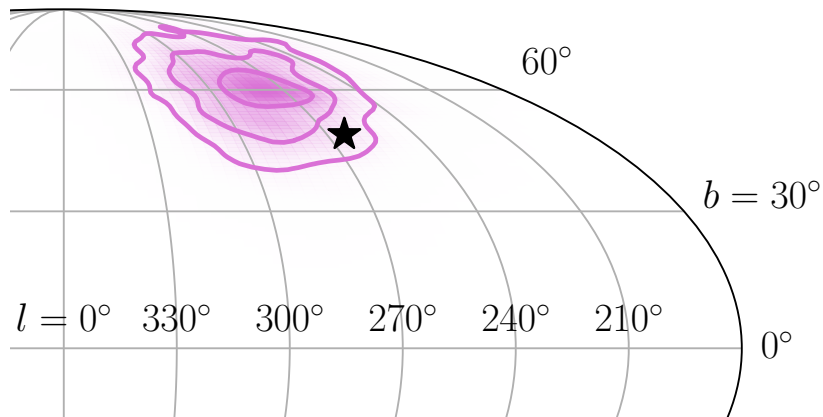


Figure 14: Projection of marginal distribution for l and b onto the sky, Galactic coordinates. ★: CMB dipole.

The Effect of Local Clustering

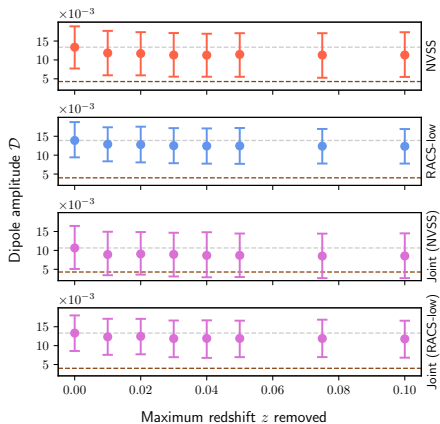


Figure 15: Inferred dipole amplitude by redshift of local source removed.

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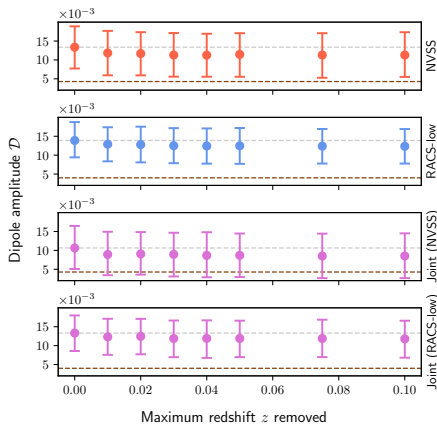


Figure 15: Inferred dipole amplitude by redshift of local source removed.

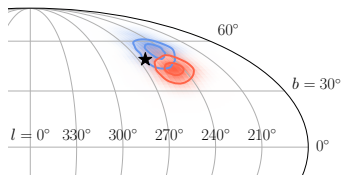


Figure 16: Inferred clustering dipole. *Star:* CMB dipole.

The Effect of Local Clustering

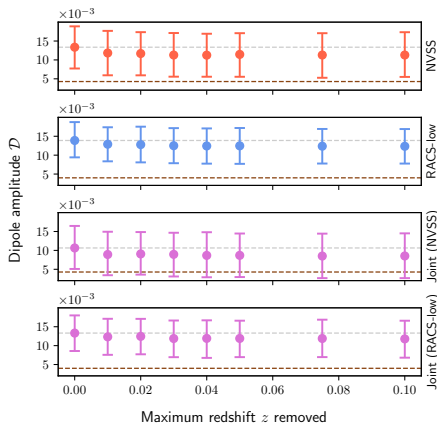


Figure 15: Inferred dipole amplitude by redshift of local source removed.

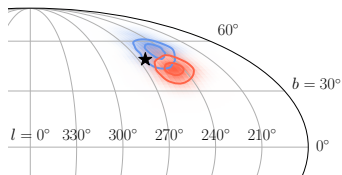


Figure 16: Inferred clustering dipole. *Star:* CMB dipole.

The clustering dipole aligns with the CMB dipole!?

NVSS and RACS Amplitudes

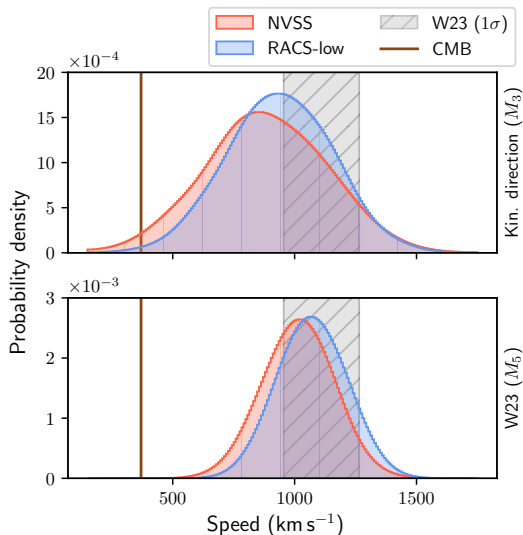


Figure 17: Marginal PDF for inferred heliocentric velocity. *Brown:* Expectation from CMB dipole. *Grey:* Results of Wagenfeld et al. (2023). *Red/blue:* Our results.

The picture is somewhat similar — an amplitude $\times 2-3$ larger than the CMB expectation is preferred.

Conclusions

Summary

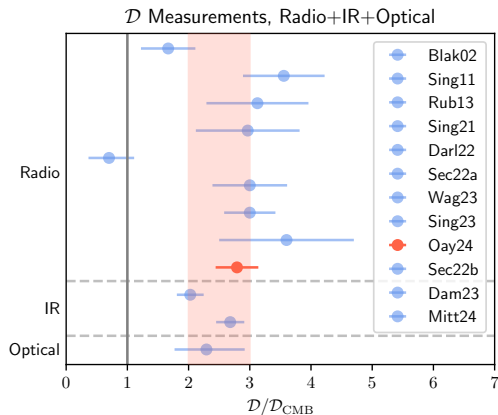


Figure 18: Literature values for \mathcal{D} including results from our work (red) and other studies (blue).

There is a trend towards an **excessive dipole** (2 to $3 \times \mathcal{D}_{\text{CMB}}$) across radio, optical and IR surveys.

This corresponds to $v \approx 1000 \text{ km s}^{-1}$, not the 370 km s^{-1} we get from the CMB.

The Hubble H_0 tension is $\approx 10\%$. This dipole tension is 100%–200% and has reached 5σ in Secret et al. (2021, 2022).

- What can we do in the future?
- Radio — RACS-mid, RACS-high?
 - Need to understand systematics better
 - There are some declination-dependent effects in RACS-mid which persist in the convolved 25" catalogue
- Other dipoles? e.g. Type Ia SNe



arXiv

*See the
paper here!*

2406.01871

What is going on? Is the cosmological principle wrong? Or are there other systematics?

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