

# Probing the cosmic dipole in galaxy surveys

ASKAP and beyond

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The University of Sydney

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Geraint Lewis  
Tara Murphy

November 21, 2024

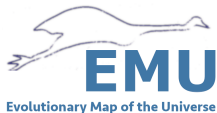


THE UNIVERSITY OF  
**SYDNEY**

EMU Cosmology  
Telecon

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November 2024



# Agenda

## Background

The Cosmological Principle  
The Ellis & Baldwin Dipole

## Analysis

Samples  
Preparation  
Statistics

## Results

Individual  
Joint

## Discussion

## Key Finding

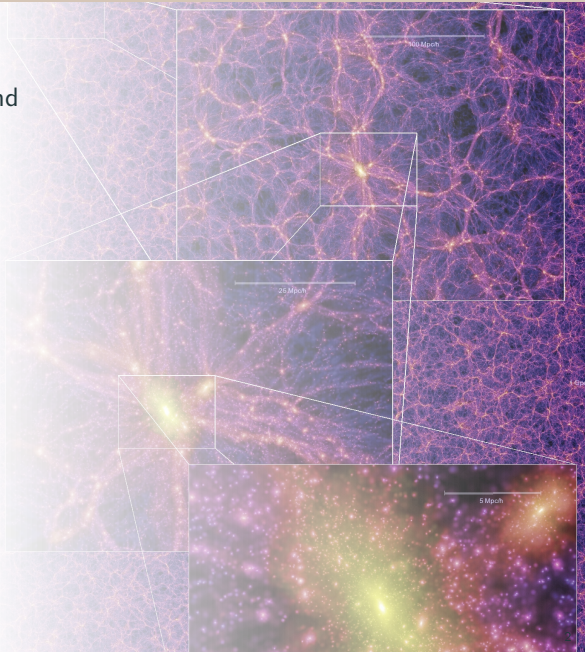
- Dipole in RACS-low & NVSS is 2 to 3 times larger than expected.
- Is the CP in trouble, or are there systematics?

# Background

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# The Cosmological Principle

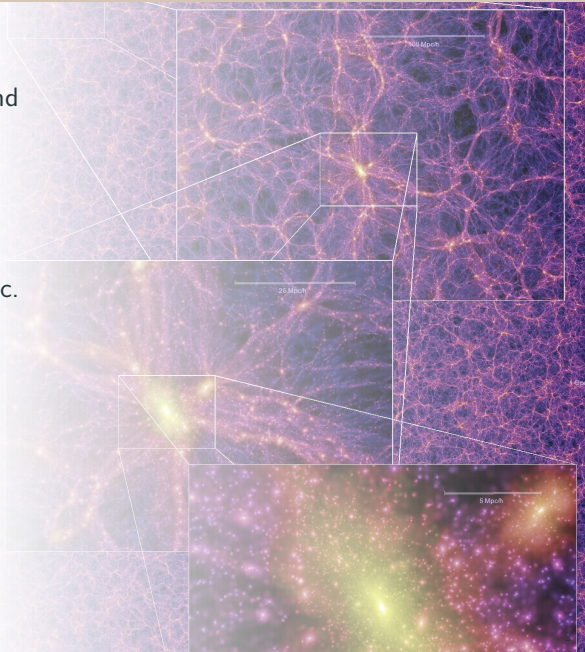
On very large scales, the Universe is **homogeneous** and **isotropic**.



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*Foundational assumption* in current cosmological framework, e.g. FLRW, Friedmann world models, etc.



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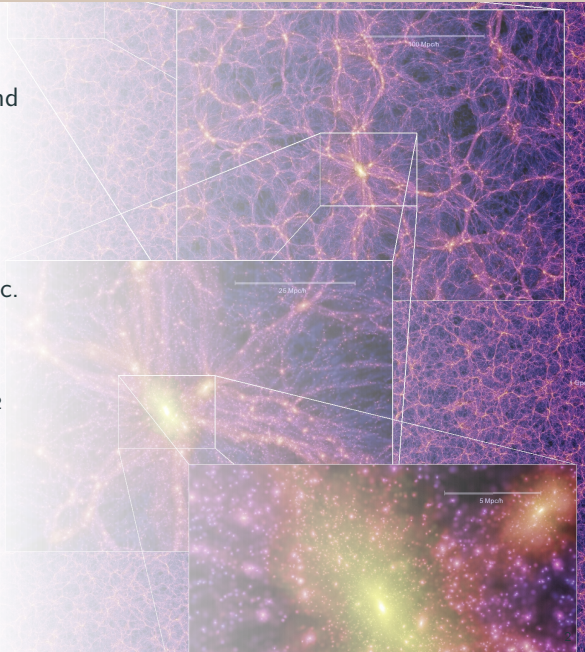
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$$ds^2 = -c^2 dt^2 + a^2(t) d\Sigma^2$$

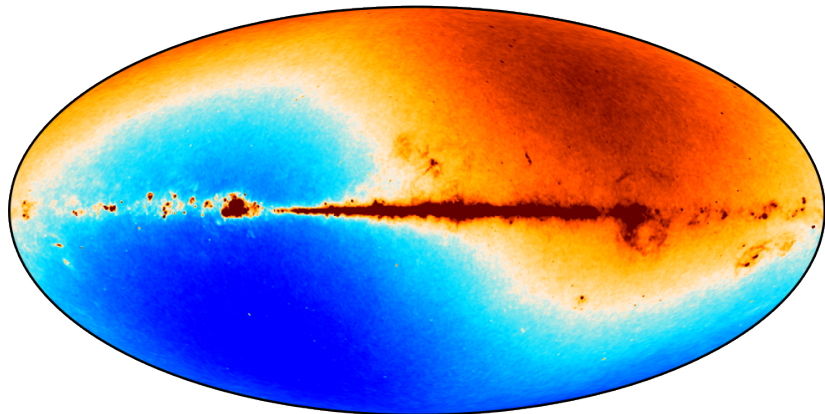
where

$$d\Sigma^2 = \frac{dr^2}{1 - \kappa r^2} + r^2 d\Omega^2$$



# The Kinematic Dipole

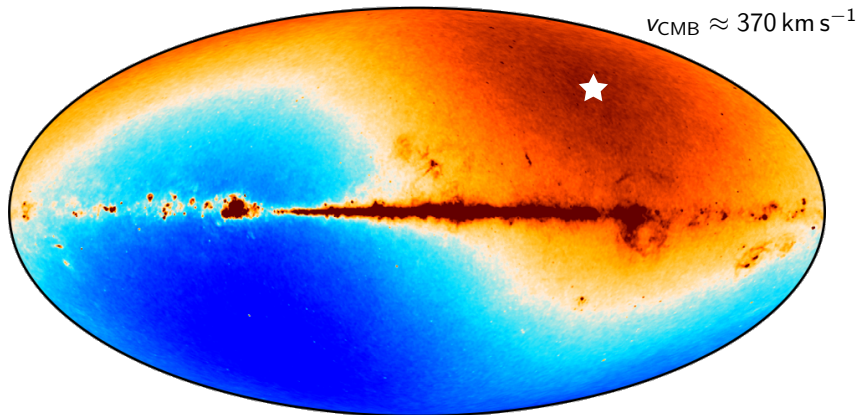
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**Figure 1:** CMB temperature map (Galactic coordinates; kinematic dipole and Galactic contamination included; BeyondPlanck). ★: dipole direction.

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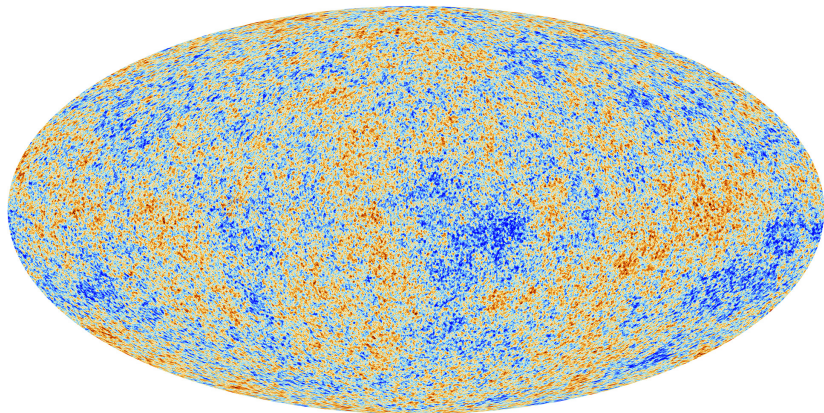
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- This is thought to be *kinematic* in origin.



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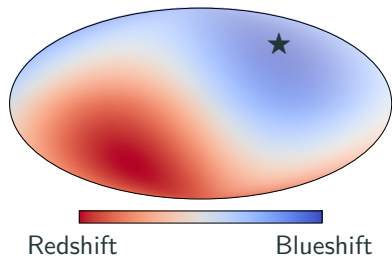
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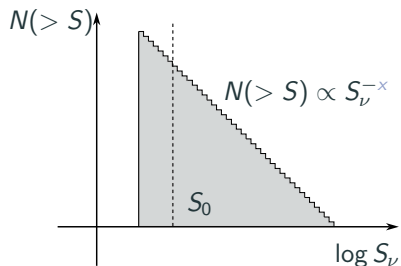


**Figure 1:** CMB temperature map (dipole excluded; Planck).

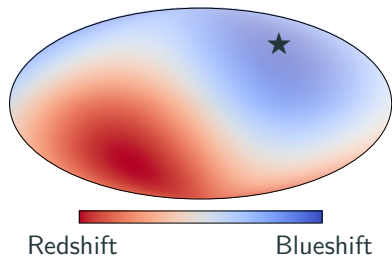
# The Ellis & Baldwin (1984) Dipole



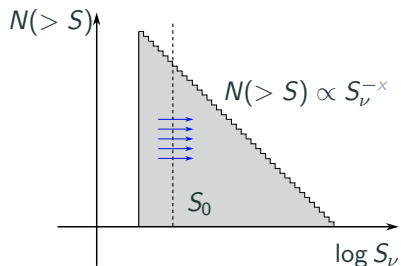
Based on special relativistic arguments, our motion induces a **dipole** in source density.



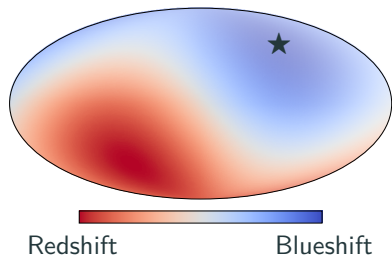
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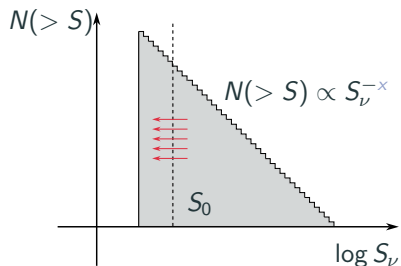
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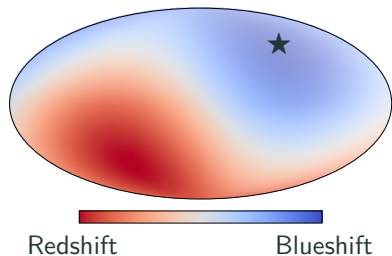
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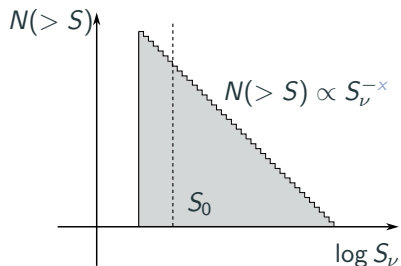
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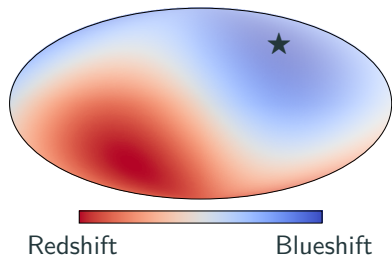
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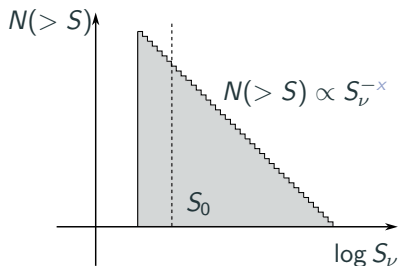
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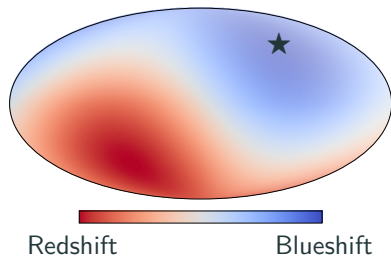
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The anticipated dipole **amplitude**:

$$\mathcal{D}_{\text{CMB}} = [2 + x(1 + \alpha)] \frac{v_{\text{CMB}}}{c}.$$



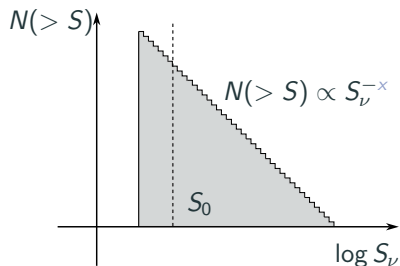
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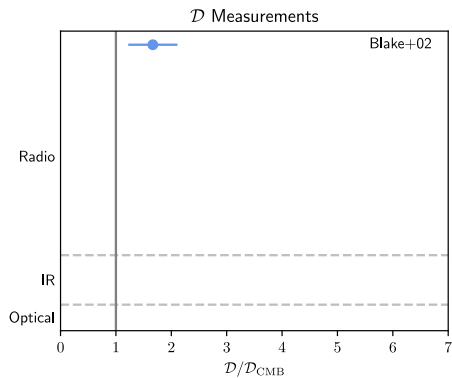
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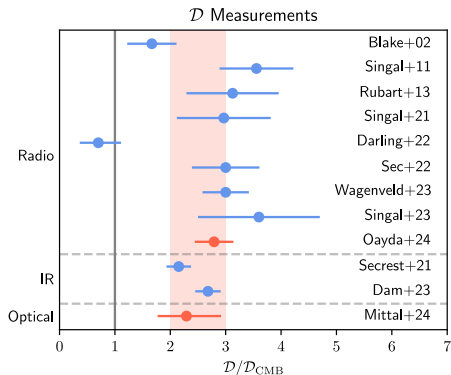


Typical values are 0.004 – 0.007.  
This is a *0.5% effect!*

# The Dipole Tension

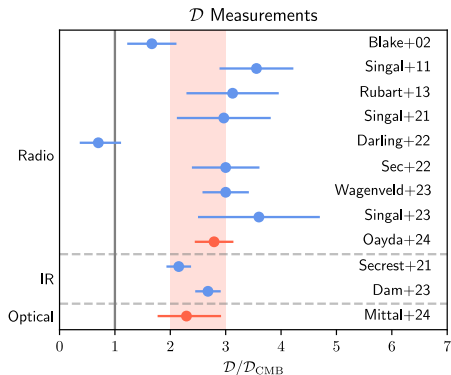


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**Figure 2:** *Top:* Literature values for  $\mathcal{D}$  ( $1\sigma$ ); our studies in red. *Right:* Dipole direction results from our studies.

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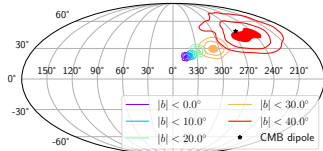


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## The cosmic dipole in the Quiaa sample of quasars: a Bayesian analysis

Vasudev Mittal<sup>1\*</sup>, Oliver T. Ouyda<sup>2,†</sup> and Geraint F. Lewis<sup>3,‡</sup>

<sup>1</sup>Department of Physical Sciences, IISER Mohali, Knowledge City, Sector 81, SAS Nagar, Mohali 140306, Punjab, India  
<sup>2</sup>Staryi Institute for Astronomy, School of Physics A28, The University of Sydney, NSW 2006, Australia

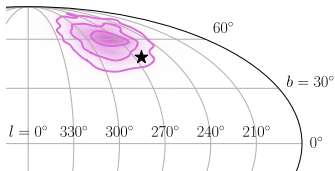


## A Bayesian approach to the cosmic dipole in radio galaxy surveys: joint analysis of NVSS & RACS

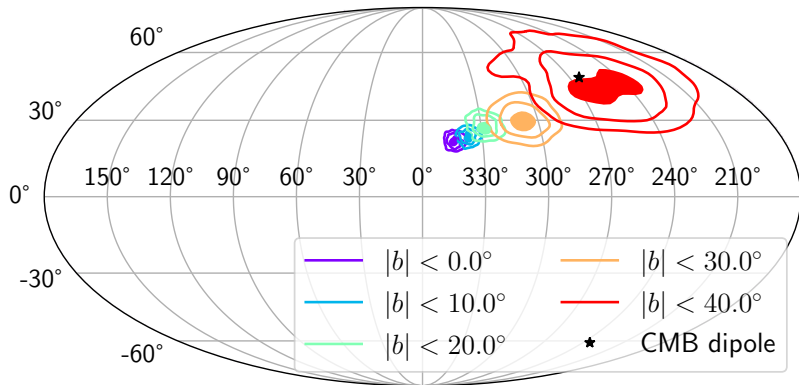
Oliver T. Ouyda<sup>1,†</sup>, Vasudev Mittal<sup>1,2</sup>, Geraint F. Lewis<sup>3,‡</sup> and Tara Murphy<sup>3,§</sup>

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<sup>2</sup>Department of Physical Sciences, IISER Mohali, Knowledge City, Sector 81, SAS Nagar, Mohali 140306, Punjab, India

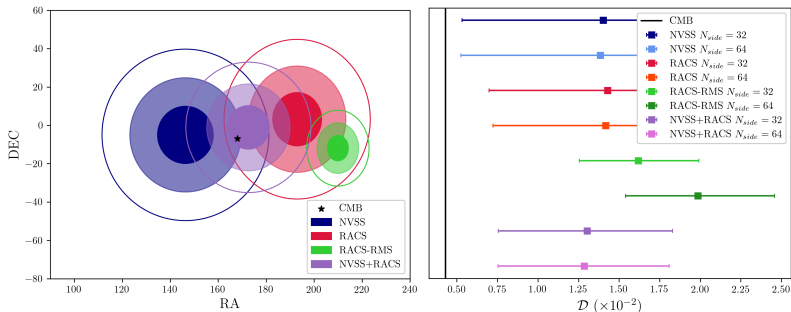


# Results of Mittal, Oayda & Lewis (2024) — Optical



**Figure 3:** Results from Quaia low ( $G < 20.0$ ) as in Mittal et al. (2024). *Top:* projection of marginal posterior for dipole direction onto the sky. *Bottom:*  $2\sigma$  credible interval for dipole amplitude by mask choice.

# Results of Wagenveld et al. (2023) — Radio



**Figure 4:** Results of Wagenveld et al. (2023) also point towards an excessive dipole amplitude (but consistent direction).

- ‘W23’ — used as prior likelihood later.
- We also analysed NVSS and RACS-low, but with a different approach.

**What is going on here? Is this a genuine tension or are there systematics?**

# Analysis

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# Samples We Tested

NVSS (NRAO VLA Sky Survey):  
1993–97, 1.4 GHz, northern sky.

RACS-low (Rapid Australian SKA  
Pathfinder Continuum Survey):  
2019–20, 887.5 MHz, southern  
sky.

**Figure 5:** *Top:* VLA in New Mexico  
(credit: NRAO). *Bottom:* Australian  
SKA Pathfinder in Western Australia  
(credit: CSIRO).



# Some Systematic Effects

Some issues to consider:



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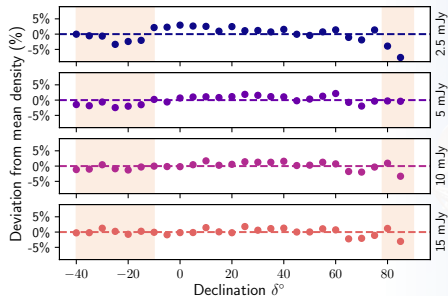
- Catalogue completeness at some  $S_\nu$ .



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Some issues to consider:

- Catalogue completeness at some  $S_\nu$ .
- Declination-dependent systematics.



**Figure 6:** Deviation from mean source density by  $\delta^\circ$  (NVSS). *Shaded brown:* DnC config.

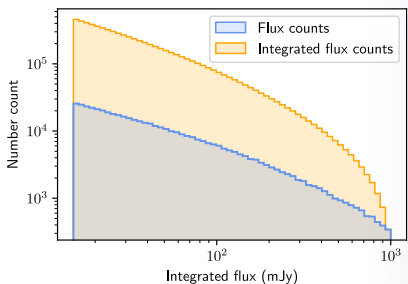
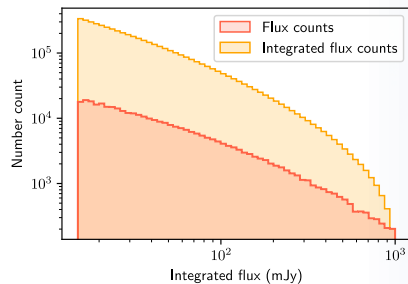
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Some issues to consider:

- Catalogue completeness at some  $S_\nu$ .
- Declination-dependent systematics.
- Contamination from the Galactic plane and bright radio sources.

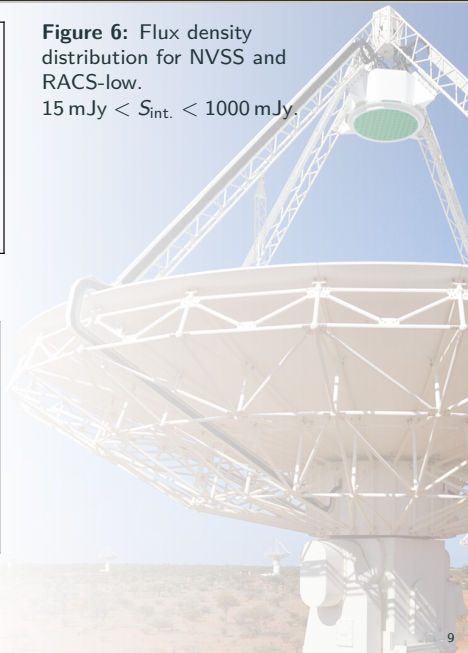


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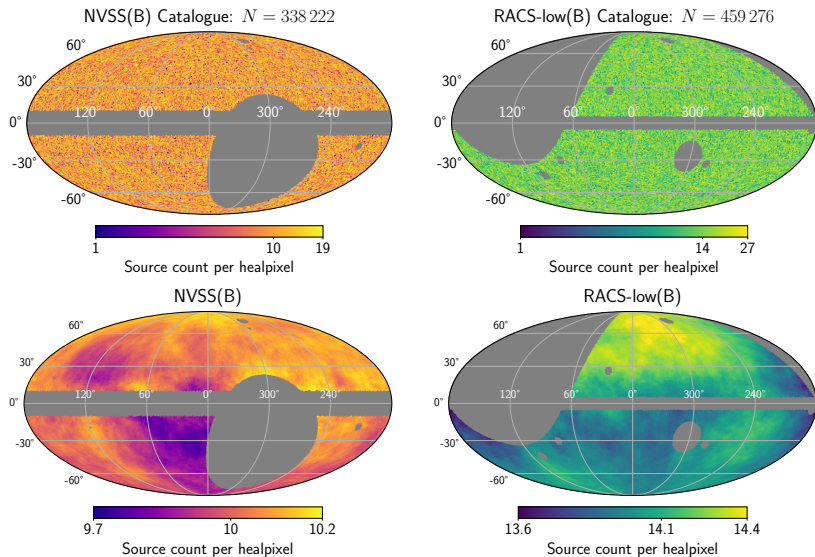


**Figure 6:** Flux density distribution for NVSS and RACS-low.

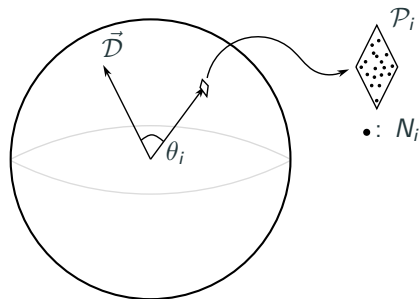
$15 \text{ mJy} < S_{\text{int.}} < 1000 \text{ mJy}$ .



# Preparing NVSS & RACS

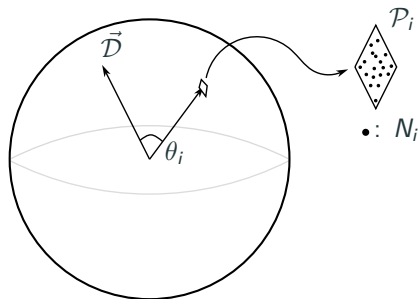


**Figure 7:** NVSS and RACS-low samples in Galactic coordinates binned into healpixels. *Top:* Raw density maps. *Bottom:* Smoothed density maps.



Dipole vector  $\vec{D}$  is a **free parameter**.

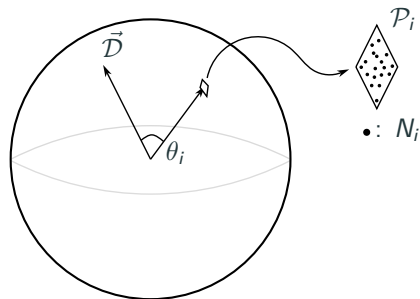
**Figure 8:** Schematic of pixel  $\mathcal{P}_i$  on the celestial sphere with  $N_i$  sources ( $\bullet$ ) near dipole vector  $\vec{D}$ .



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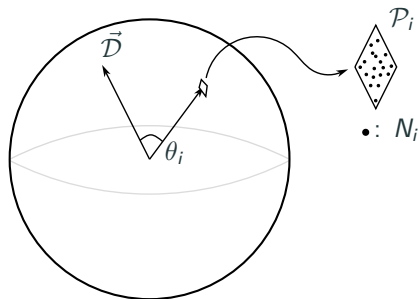
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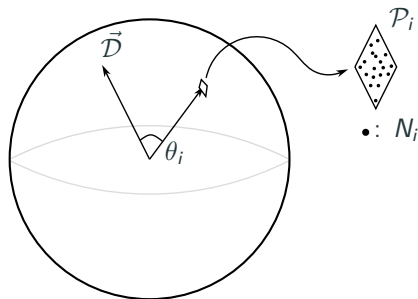
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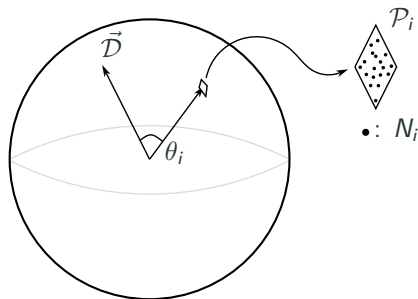
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Use a **Bayesian** statistical approach to infer posterior probability distribution for  $\Theta = \{\mathcal{D}, l, b\}$ . Analyse individually and **jointly**.

# Model Comparison

	<b>Short label</b>	<b>Description</b>
$M_0$	Null	Monopole
$M_1$	Free dipole	Free $\mathcal{D}$ , $l$ , $b$
$M_2$	Kinematic velocity	$\mathcal{D}$ fixed and free $l$ , $b$
$M_3$	Kinematic direction	$l$ , $b$ fixed and free $\mathcal{D}$
$M_4$	Kinematic dipole	All parameters fixed to CMB expectation
$M_5$	W23	$\mathcal{D}$ , $l$ , $b$ from Wagenveld et al. (2023)

**Table 1:** The six models tested and ranked.

Compare models' explanatory power with **marginal likelihood**  $\mathcal{Z}(\mathbf{D}|M)$ .

This gives us the Bayes factor  $\ln B_{i0} = \ln \mathcal{Z}_i - \ln \mathcal{Z}_0$ .

## Results

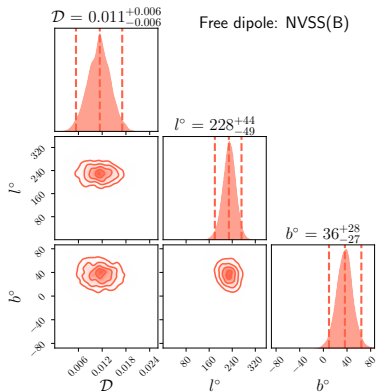
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## NVSS & RACS: Individual Results

$$\mathcal{D}_{\text{CMB}} \approx 0.004$$

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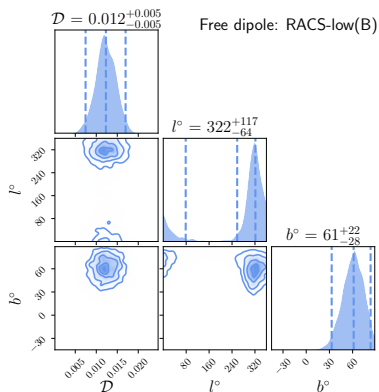
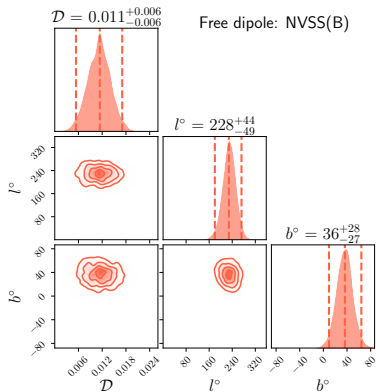
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Model	$\ln B_{i0}$
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$M_3$ Kin. direction	4.5
$M_4$ Kin. dipole	4.8 🏆

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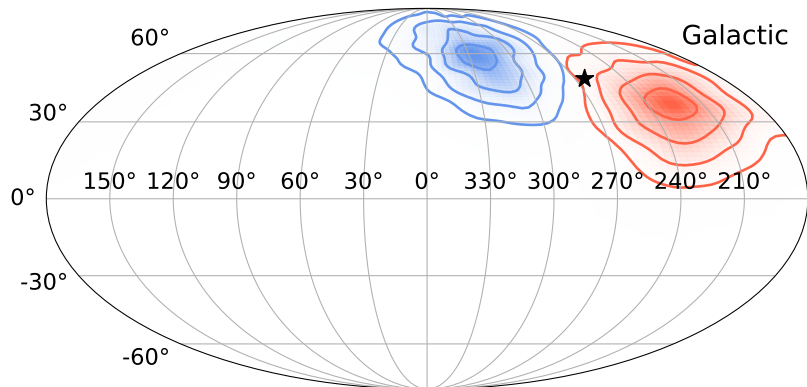
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Model	$\ln B_{l0}$
$M_1$ Free dipole	3.1
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$M_4$ Kin. dipole	4.8 

Model	$\ln B_{l0}$
$M_1$ Free dipole	8.2 
$M_3$ Kin. direction	7.5
$M_4$ Kin. dipole	6.6

# NVSS & RACS: Individual Results



**Figure 9:** Projection of distribution for  $l$  and  $b$  onto the sky (Galactic coordinates) for RACS-low and NVSS.  $\star$ : CMB dipole.

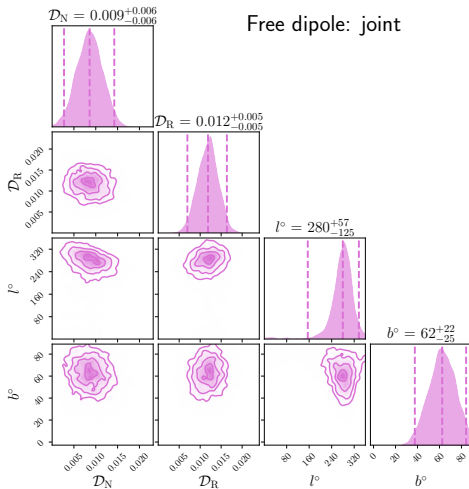
$$\mathcal{D}_{\text{NVSS}} \approx (11 \pm 6) \times 10^{-3} \quad \mathcal{D}_{\text{RACS}} \approx (12 \pm 5) \times 10^{-3}$$

## Joint Analysis: NVSS + RACS-low

$$\mathcal{D}_{\text{CMB}} \approx 0.004 \quad - \quad \ln \mathcal{L} = \ln \mathcal{L}_{\text{NVSS}} + \mathcal{L}_{\text{RACS}}$$

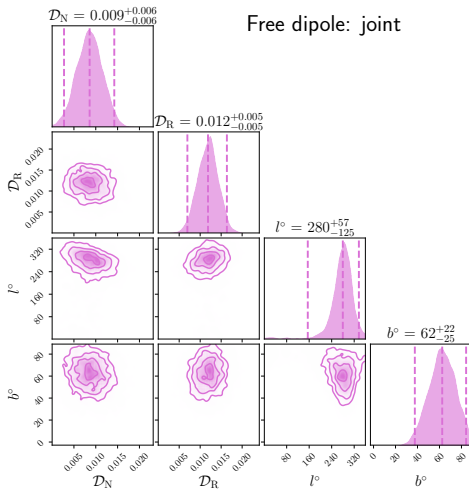
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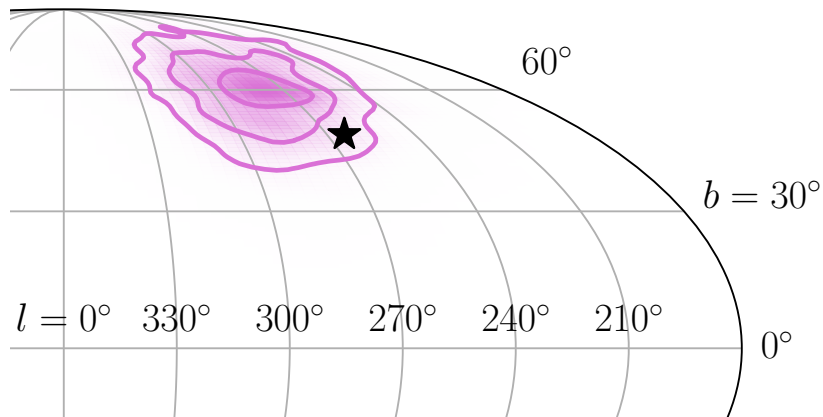
Model		$\ln B_{i0}$
$M_3$	Kin. dir.	12.1 
$M_4$	Kin. dipole	11.4
$M_5$	W23	17.1 

$M_3$  (kinematic direction):

$$\mathcal{D}_{\text{NVSS}} \approx (10 \pm 5) \times 10^{-3}$$

$$\mathcal{D}_{\text{RACS}} \approx (11 \pm 5) \times 10^{-3}$$

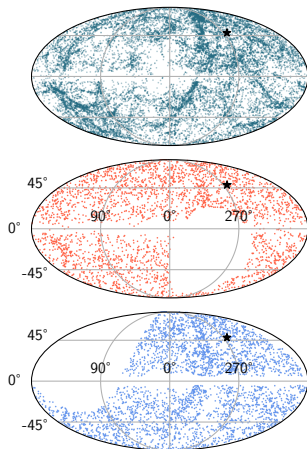
## Joint Analysis: Dipole Position Distribution



**Figure 10:** Projection of marginal distribution for  $l$  and  $b$  onto the sky, Galactic coordinates. ★: CMB dipole.

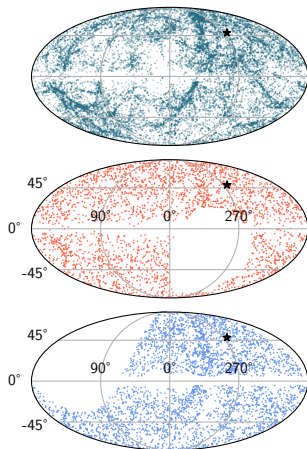
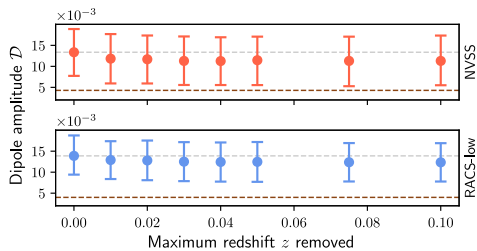
# Clustering & Local Sources

Figure 11: ★: CMB dipole. *Red*: Results for NVSS. *Blue*: Results for RACS-low.



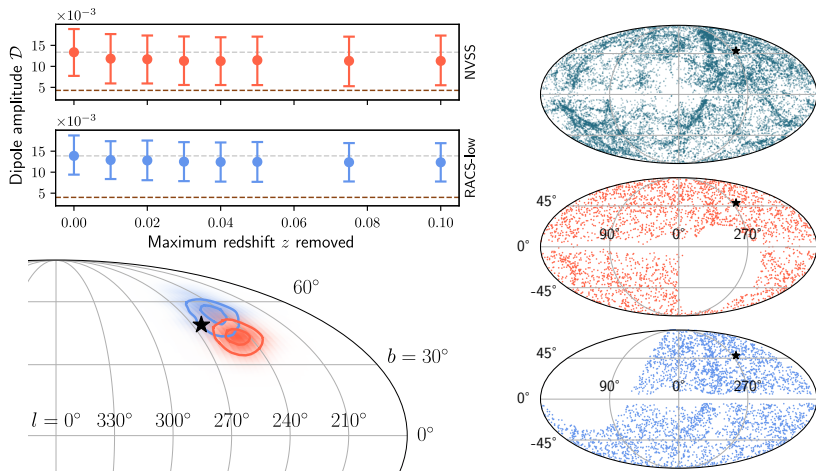
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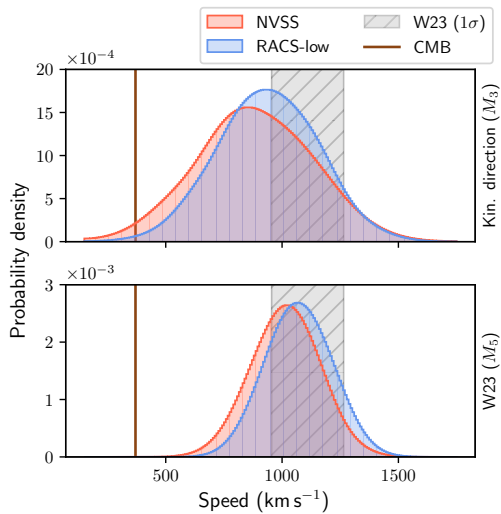
Figure 11: ★: CMB dipole. *Red*: Results for NVSS. *Blue*: Results for RACS-low.



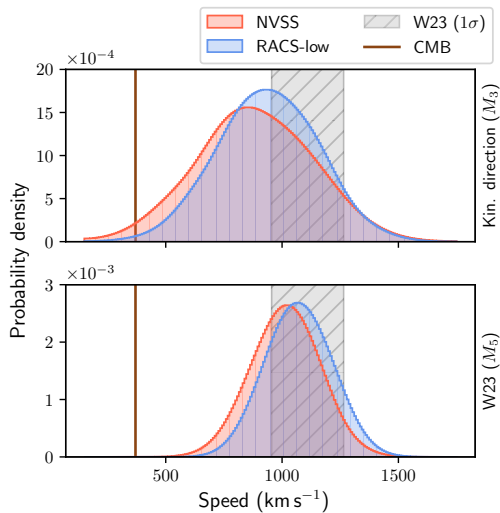
## Discussion

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# Summary

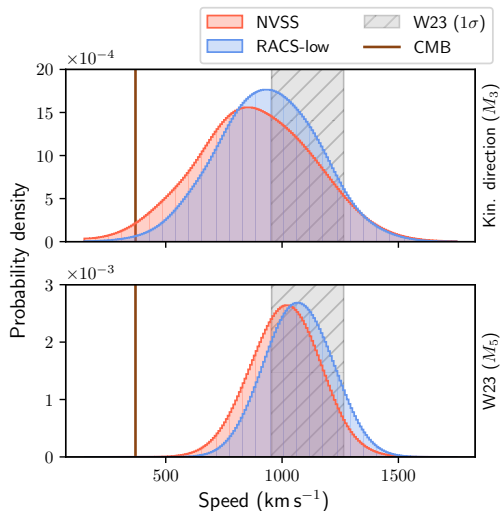


# Summary



There is evidence for an **excessive dipole** in RACS/NVSS ( $2$  to  $3 \times \mathcal{D}_{\text{CMB}}$ ).

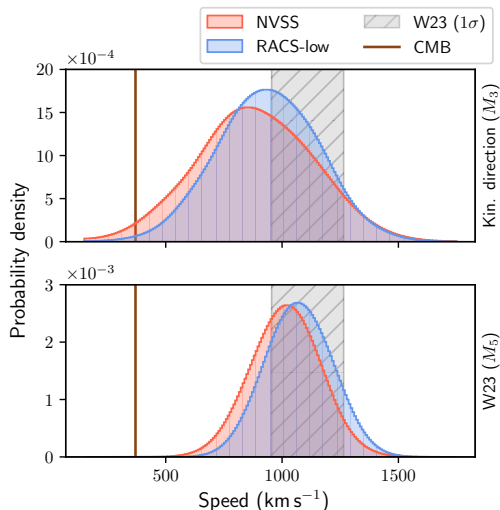
# Summary



There is evidence for an **excessive dipole** in RACS/NVSS (2 to  $3 \times \mathcal{D}_{\text{CMB}}$ ).

This corresponds to  **$v \approx 1000 \text{ km s}^{-1}$** , not  $v_{\text{CMB}} \approx 370 \text{ km s}^{-1}$ .

# Summary



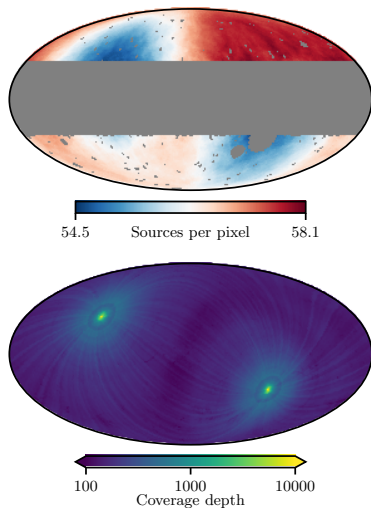
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The Hubble  $H_0$  tension is  $\approx 10\%$ . This dipole tension is  $100\%$ – $200\%$  and has reached  $5\sigma$  (see e.g. Secrest et al., 2021; Dam et al., 2023).

# The Future — Investigating Systematics

The CatWISE2020 sample used in Se-crest et al. (2021) has been questioned by Abghari et al. (2024).

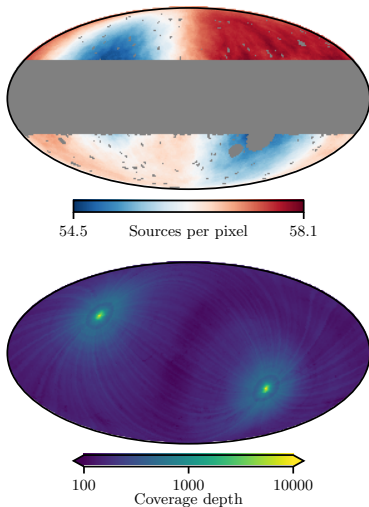
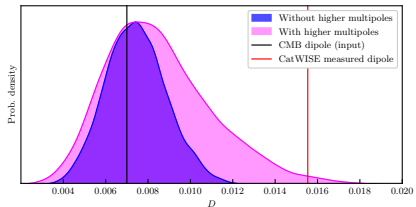


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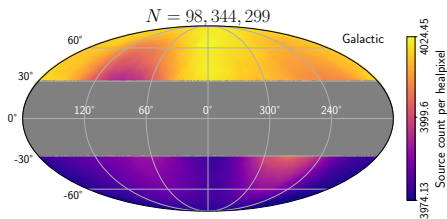
What if there are additional, higher order multipoles on a masked sky? **Mode coupling; power leakage.**

**Figure 12:** Plots from Abghari et al. (2024). *Right:* Smoothed CatWISE density map & scanning law. *Bottom:* Effect of additional multipoles on  $\mathcal{D}$ .



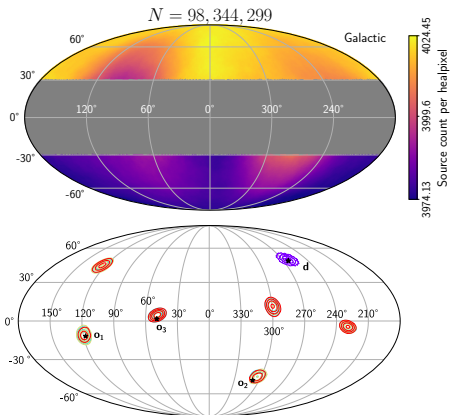
# Dipole & Octupole

**Figure 13:** Results from fit to synthetic sample with intrinsic dipole ( $\ell = 1$ ) and octupole ( $\ell = 3$ ; Oayda et al., submitted).



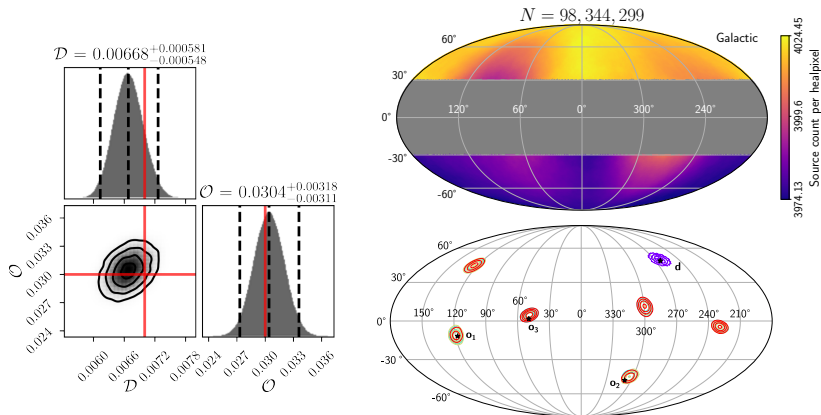
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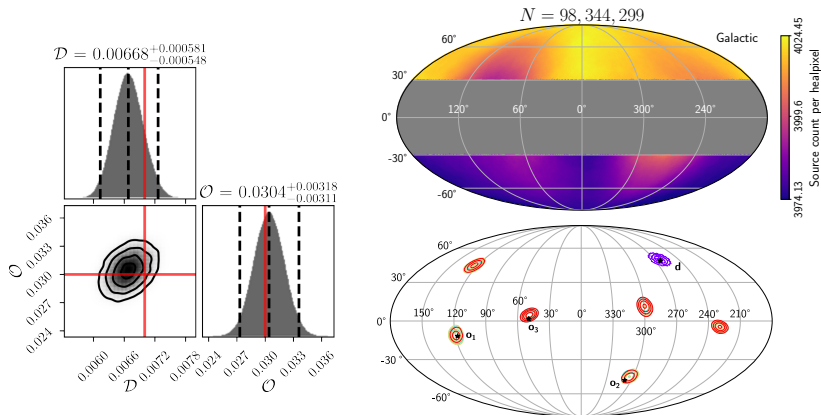
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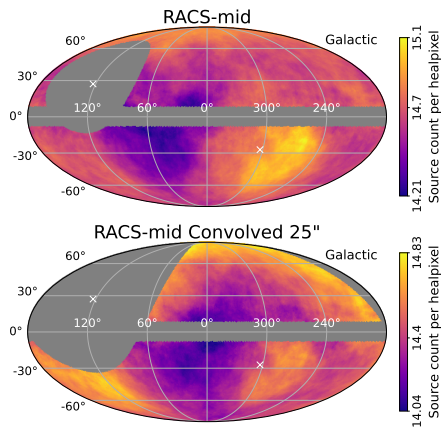
The dipole & octupole are disentangled from each other!

# Why Multipoles?

We can use this approach as a diagnostic tool. For example...

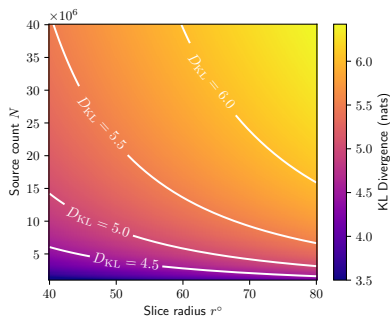
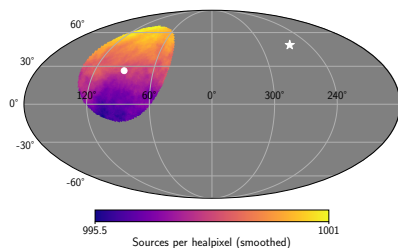
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**Figure 14:**  
 $10 \text{ mJy} < S_{\text{int.}} < 1000 \text{ mJy}$ .  
Smoothed RACS-mid maps  
(Galactic coordinates). *Top:*  
RACS-mid. *Bottom:* RACS-mid  
convolved to 25" common  
resolution.

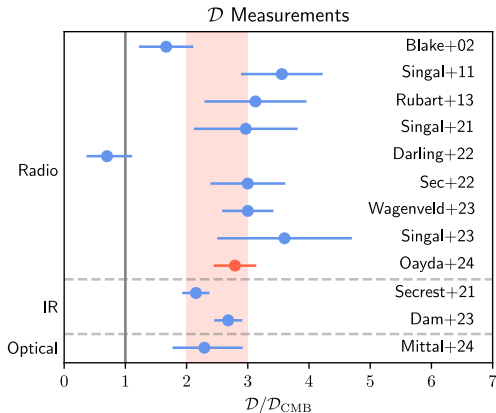
# Optimising Surveys



We're thinking about how our inferences change with surveys of different source counts and sky coverages.

EMU's anticipated  $\approx 70$  million sources (Norris et al., 2011) will be more than sufficient.

# Conclusions



**Figure 15:** Literature values for  $\mathcal{D}$  including results from our work (red) with RACS-low & NVSS and other studies (blue).

## Key Finding

- RACS-low & NVSS dipole about a factor of 2 to 3 too large.
- We have to seriously investigate possible systematics.

# References

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